

# Stage 6 PROMPT sheet

## 6/1 Place value in numbers to 10million

The position of the digit gives its size

Ten millions	Millions	Hundred thousands	Ten thousands	thousands	hundreds	tens	units
1	2	3	4	5	6	7	8

### Example

The value of the digit '1' is 10 000 000

The value of the digit '2' is 2 000 000

The value of the digit '3' is 300 000

The value of the digit '4' is 40 000

## 6/1 Round whole numbers

**Example 1** - Round 342 679 to the nearest 10 000

- Step 1 - Find the 'round-off digit' - 4
- Step 2 - Move one digit to the right - 2

4 or less? YES - leave 'round off digit' unchanged  
- Replace following digits with zeros

ANSWER - 340 000

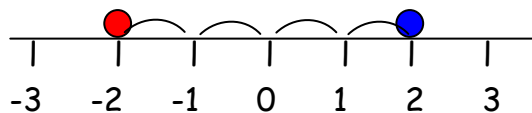
**Example 2** - Round 345 679 to the nearest 10 000

- Step 1 - Find the 'round-off digit' - 4
- Step 2 - Move one digit to the right - 5

5 or more? YES - add one to 'round off digit'  
- Replace following digits with zeros

ANSWER - 350 000

## 6/2 Negative numbers



$2 > -2$  → We say 2 is bigger than -2

$-2 < 2$  → We say -2 is less than 2

The difference between 2 and  $-2 = 4$  (see line)

Remember the rules:

- When subtracting go down the number line
- When adding go up the number line
- $8 + -2$  is the same as  $8 - 2 = 6$
- $8 - +2$  is the same as  $8 - 2 = 6$
- $8 - -2$  is the same as  $8 + 2 = 10$

## 6/3 Multiply numbers & estimate to check

e.g.  $152 \times 34$

### COLUMN METHOD

$$\begin{array}{r} 152 \\ 34 \times \\ \hline 608 \quad (\times 4) \\ 4560 \quad (\times 30) \\ \hline 5168 \end{array}$$

### 6/3 Use estimates to check calculations

$$\begin{array}{l} 152 \times 34 \\ \approx 150 \times 30 \\ \approx 4500 \end{array}$$

$\approx$  is the symbol for 'roughly equals'

## 6/3 Divide numbers & estimate to check

With a remainder also expressed as a fraction

e.g.  $4928 \div 32$

### BUS SHELTER METHOD

$$\begin{array}{r} 028 \\ 15 \overline{) 432} \\ \underline{-30} \phantom{0} \\ 132 \\ \underline{-120} \\ 12 \end{array}$$

$$15 \overline{) 432} \text{ r } 12$$

ANSWER -  $432 \div 15 = 28 \text{ r } 12$

$$= 28 \frac{12}{15}$$

### 6/3 continued

With a remainder expressed as a decimal

$$\begin{array}{r} 028.8 \\ 15 \overline{)432.0} \\ \underline{-30} \phantom{0} \\ 132 \\ \underline{-120} \\ 12 \end{array} \qquad \begin{array}{r} 028.8 \\ 15 \overline{)4^4 3^{13} 2.^{12} 0} \end{array}$$

ANSWER -  $432 \div 15 = 28.8$

### 6/3 Use estimates to check calculations

$432 \div 15$   
 $\approx 450 \div 15$   
 $\approx 30$

### 6/4 Factors, multiples & primes

- FACTORS** are what divides exactly into a number

e.g. Factors of 12 are:      Factors of 18 are:

1	12	1	18
2	6	2	9
3	4	3	6

The common factors of 12 & 18 are: 1, 2, 3, 6,  
The Highest Common Factor is: 6

- PRIME NUMBERS** have only TWO factors

e.g. Factors of 7 are:      Factors of 13 are

1	7	1	13
---	---	---	----

So 7 and 13 are both prime numbers

- MULTIPLES** are the times table answers

e.g. Multiples of 5 are:      Multiples of 4 are:  

5	10	15	20	25	.....
---	----	----	----	----	-------

4	8	12	16	20	.....
---	---	----	----	----	-------

The Lowest Common Multiple of 5 and 4 is: 20

### 6/5 Order of operations

- B**racket
  - I**ndices
  - D**ivide
  - M**ultiply
  - A**dd
  - S**ubtract
- } Do these in the order they appear
- } Do these in the order they appear

e.g.  $3 + 4 \times 6 - 5 = 22$

$(2 + 1) \times 3 = 9$   
 ↑ first  
 ↑ first

### 6/6 Addition

- Line up the digits in the correct columns**

e.g.  $48p + \pounds 2.84 + \pounds 9$

$$\begin{array}{r} 0.48 \\ 2.84 \\ 9.00+ \\ \hline \pounds 12.32 \\ 111 \end{array}$$

### 6/6 Subtraction

- Line up the digits in the correct columns**

e.g.  $645 - 427$

			H	T	U
	6	4	5		
	4	2	7		
	2	1	8		

### 6/7 Equivalent fractions

- To simplify a fraction

Example:  $\frac{27}{36}$

First find the highest common factor of the numerator and denominator - which is 9, then divide

$$\frac{27 \div 9}{36 \div 9} = \frac{3}{4}$$

- To change fractions to the same denominator

Example:  $\frac{3}{4}$  and  $\frac{2}{3}$

Find the highest common multiple of the denominators - which is 12, then multiply:

$$\frac{3 \times 3}{4 \times 3} = \frac{9}{12} \quad \text{and} \quad \frac{2 \times 4}{3 \times 4} = \frac{8}{12}$$

## 6/8 Add & subtract fractions

- Make the denominators the same

<p>e.g. <math>\frac{1}{5} + \frac{7}{10}</math></p> $= \frac{2}{10} + \frac{7}{10}$ $= \frac{9}{10}$	<p>e.g. <math>\frac{4}{5} - \frac{2}{3}</math></p> $= \frac{12}{15} - \frac{10}{15}$ $= \frac{2}{15}$
--	---

Do not add denominators

- To **multiply by 10**, move each digit one place to the left  
e.g.  $35.6 \times 10 = 356$

Hundreds	Tens	Units	•	tenths
	3	5	•	6
3	5	6	•	

- To **divide by 10**, move each digit one place to the right

e.g.  $35.6 \div 10 = 3.56$

Tens	Units	•	tenths	hundredths
3	5	•	6	
	3	•	5	6

- To **multiply by 100**, move each digit 2 places to the left
- To **divide by 100**, move each digit 2 places to the right

### AN ALTERNATE METHOD

Instead of moving the digits  
Move the decimal point the opposite way

## 6/9 Multiply fractions

- Write 5 as  $\frac{5}{1}$
- Multiply numerators & denominators

<p>e.g. <math>5 \times \frac{2}{3}</math></p> $= \frac{5}{1} \times \frac{2}{3}$ $= \frac{10}{3} = 3\frac{1}{3}$	<p>e.g. <math>\frac{4}{5} \times \frac{2}{3}</math></p> $= \frac{8}{15}$
--	--

## 6/9 Divide fractions

- Write 5 as  $\frac{5}{1}$
- Invert the fraction after  $\div$  sign
- Multiply numerators & denominators

<p>e.g. <math>\frac{2}{3} \div 5</math></p> $= \frac{2}{3} \times \frac{1}{5}$ $= \frac{2}{15}$	<p>e.g. <math>\frac{4}{5} \div \frac{2}{3}</math></p> $= \frac{4}{5} \times \frac{3}{2}$ $= \frac{12}{10} = 1\frac{2}{10} = 1\frac{1}{5}$
---	---

## 6/10 Multiply/divide decimals by 10, 100

thousands	hundreds	tens	units	•	tenths	hundredths	thousandths
4	3	5	2	•	6	1	7

## 6/11 Multiply decimals

- Step 1 - remove the decimal point
- Step 2 - multiply the two numbers
- Step 3 - Put the decimal back in

Example:  $0.06 \times 8$

$$\Rightarrow 6 \times 8$$

$$\Rightarrow 48$$

$$\Rightarrow 0.48$$

## 6/11 Divide decimals

- Use the bus shelter method
- Keep the decimal point in the same place
- Add zeros for remainders

Example:  $6.28 \div 5$

$$\begin{array}{r} 1.256 \\ 5 \overline{) 6.280} \end{array}$$

## 6/12 Fraction, decimal, percentage equivalents

### LEARN THESE:

$$\frac{1}{4} = 0.25 = 25\%$$

$$\frac{1}{2} = 0.5 = 50\%$$

$$\frac{3}{4} = 0.75 = 75\%$$

$$\frac{1}{10} = 0.1 = 10\%$$

### Percentage to decimal to fraction

$$27\% = 0.27 = \frac{27}{100}$$

$$7\% = 0.07 = \frac{7}{100}$$

$$70\% = 0.7 = \frac{70}{100} = \frac{7}{10}$$

### Decimal to percentage to fraction

$$0.3 = 30\% = \frac{3}{10}$$

$$0.03 = 3\% = \frac{3}{100}$$

$$0.39 = 39\% = \frac{39}{100}$$

### Fraction to decimal to percentage

$$\frac{4}{5} = \frac{80}{100} = 80\% = 0.8$$

Change to 100

0.375

$$\frac{3}{8} = 3 \div 8 = 8) 3.306040 = 0.375 = 37.5\%$$

$$\frac{9}{12} = \frac{3}{4} = 0.75 = 75\%$$

Cancel by 3

## 6/13 Fraction of quantity

- $\frac{4}{5}$  means  $\div 5 \times 4$

e.g. To find  $\frac{4}{5}$  of £40

$$£40 \div 5 \times 4 = £40$$

## 6/13 Percentage of quantity

Use only

- 50% -  $\frac{1}{2}$
- 10% -  $\frac{1}{10}$
- 1% -  $\frac{1}{100}$

Example : To find 35% of £400

$$10\% = £40$$

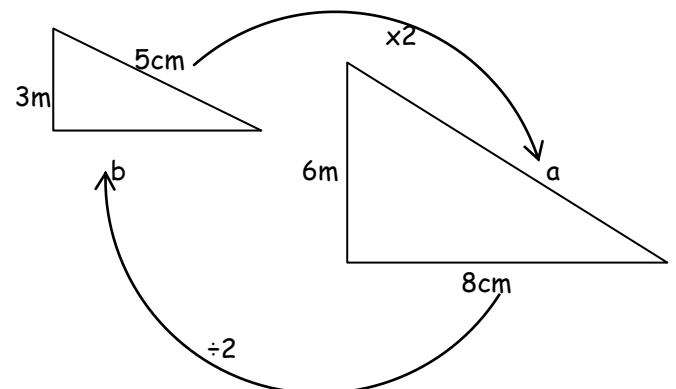
$$20\% = £80$$

$$5\% = £20$$

$$35\% = £140$$

## 6/14 Similar shapes

When a shape is enlarged by a scale factor the two shapes are called SIMILAR shapes



$$\text{Scale factor} = 6 \div 3 = 2$$

$$\text{Length } a = 5 \times 2 = 10\text{cm}$$

$$\text{Length } b = 8 \div 2 = 4\text{cm}$$

## 6/14 Unequal sharing

Example- unequal sharing of sweets

A gets

B gets

3 shares

4 shares

=> 3 sweets

4 sweets

=> 12 sweets

16 sweets

x4

x4

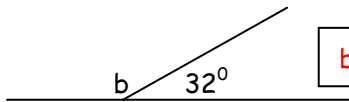
**6/15 Express missing numbers algebraically**

An unknown number is given a letter

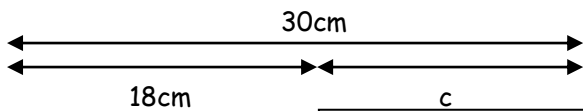
**Examples**

$2a - 4 = 8$

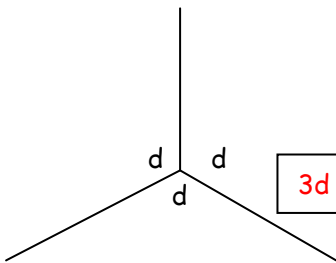
$2a = 12$  so  $a = 6$



$b + 32 = 180$  so  $b = 148^\circ$



$18 + c = 30$  so  $c = 12$



$3d = 360^\circ$  so  $d = 120^\circ$

**6/15 Use a word formula**

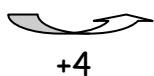
**Example: - Time to cook a turkey**  
Cook for 45min per kg weight  
Then a further 45min

For a 6kg turkey, follow the formula:  
 $45\text{min} \times 6 + 45\text{min}$   
 $= 270\text{min} + 45\text{min}$   
 $= 315\text{min}$   
 $= 5\text{h } 15\text{min}$

**6/16 Number sequences**

- Understand position and term

Position	1	2	3	4
Term	3	7	11	15



Term to term rule = **+4**  
Position to term rule is  $n \times 4 - 1$   
(because position 1  $\times 4 - 1 = 3$ )  
nth term =  $n \times 4 - 1 = 4n - 1$

- Generate terms of a sequence

If the nth term is  $5n + 1$   
1<sup>st</sup> term ( $n=1$ ) =  $5 \times 1 + 1 = 6$   
2<sup>nd</sup> term ( $n=2$ ) =  $5 \times 2 + 1 = 11$   
3<sup>rd</sup> term ( $n=3$ ) =  $5 \times 3 + 1 = 16$

**6/17 Possible solutions of a number sentence**

Example: x and y are numbers  
Rule:  $x + y = 5$   
Possible solutions:  $x = 0$  and  $y = 5$   
 $x = 1$  and  $y = 4$   
 $x = 2$  and  $y = 3$   
 $x = 3$  and  $y = 2$   
 $x = 4$  and  $y = 1$   
 $x = 5$  and  $y = 0$

**6/18 Convert units of measure METRIC**

When converting measurements follow these rules:  
• When converting from a **larger unit to a smaller** unit we **multiply** ( $\times$ )  
• When converting from a **smaller unit to a larger** unit we **divide** ( $\div$ )

**UNITS of LENGTH**

10mm = 1cm  
100cm = 1m  
1000m = 1km

**UNITS of MASS**

1000g = 1kg  
1000kg = 1tonne

**UNITS of VOLUME**

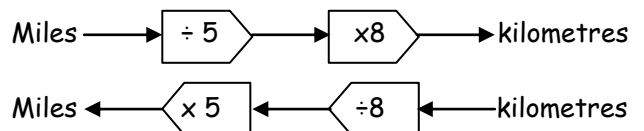
1000ml = 1 litre  
100cl = 1litre

**UNITS of TIME**

60sec = 1 min  
60min = 1 hour  
24h = 1 day  
365days = 1 year

**6/19 Convert units of measure METRIC/IMPERIAL**

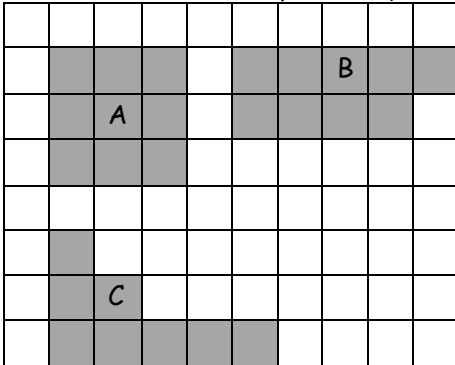
LEARN: 5 miles = 8km



## 6/20 Perimeter and area of shapes

Shapes can have the SAME area but different perimeters

The area of each shape is 9 squares

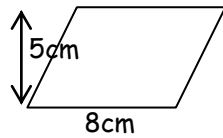


Perimeter of each shape is different  
A - 12; B - 14; C - 16

## 6/21 Area of parallelogram & triangle

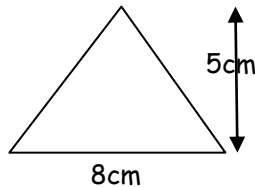
○ **Area of parallelogram**

$$\begin{aligned} \text{Area of parallelogram} &= b \times h \\ &= 8 \times 5 \\ &= \underline{40\text{cm}^2} \end{aligned}$$



○ **Area of triangle ( $\frac{1}{2}$  a parallelogram)**

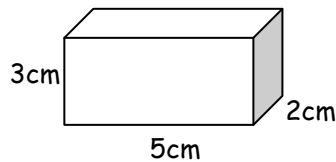
$$\begin{aligned} \text{Area of triangle} &= \frac{b \times h}{2} \\ &= \frac{8 \times 5}{2} \\ &= \underline{20\text{cm}^2} \end{aligned}$$



## 6/22 Volume

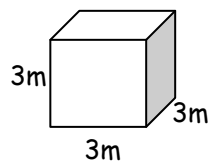
○ **Volume of cuboid**

$$\begin{aligned} \text{Volume} &= l \times w \times h \\ &= 5 \times 3 \times 2 \\ &= 30\text{cm}^3 \end{aligned}$$



○ **Volume of cube**

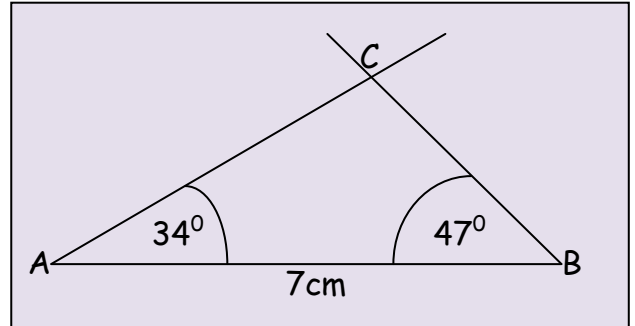
$$\begin{aligned} \text{Volume} &= l \times w \times h \\ &= 3 \times 3 \times 3 \\ &= 27\text{m}^3 \end{aligned}$$



## 6/23 Construct 2D shapes

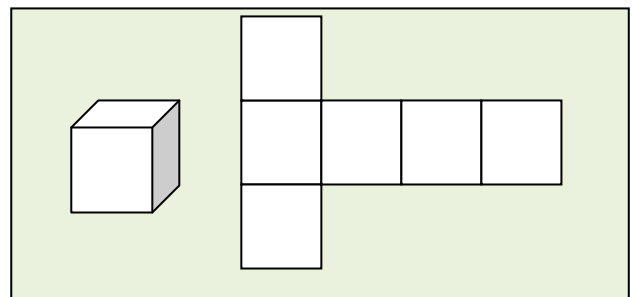
Example : Triangle with side and angles given

- Draw line AB = 7cm
- Draw angle  $34^\circ$  at point A from line AB
- Draw angle  $47^\circ$  at point B from line AB
- Extend to intersect the lines at C

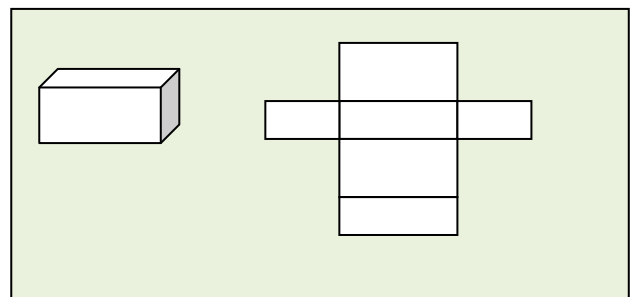


## 6/23 Construct 3D shapes

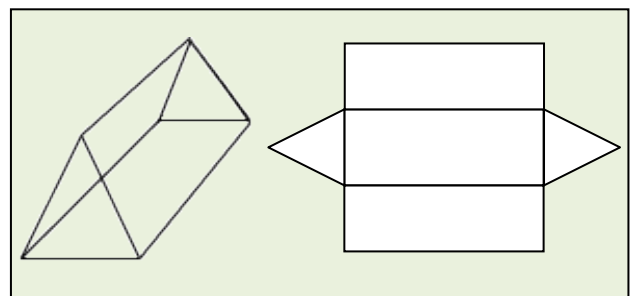
### CUBE & its net



### CUBOID & its net



### TRIANGULAR PRISM & its net

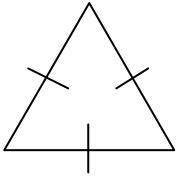


## 6/24 Properties of shapes

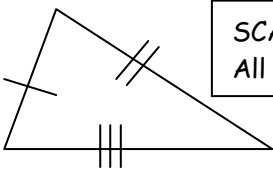
### TRIANGLES - sum of angles = $180^\circ$



ISOSCELES triangle  
2 equal sides & 2 equal angles

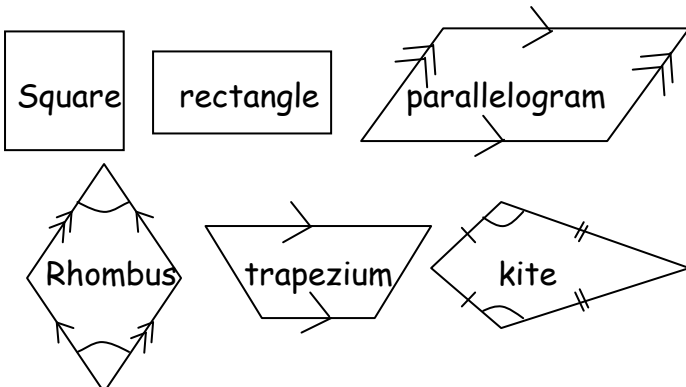


EQUILATERAL triangle  
3 equal sides & ALL angles  $60^\circ$



SCALENE triangle  
All sides & angles different

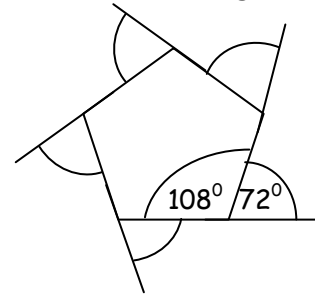
### QUADRILATERALS - sum of angles = $360^\circ$



### REGULAR POLYGONS - all sides the same

- Polygons have straight sides
- Polygons are named by the number sides
  - 3 sides - triangle
  - 4 sides - quadrilateral
  - 5 sides - pentagon
  - 6 sides - hexagon
  - 7 sides - heptagon
  - 8 sides - octagon
  - 9 sides - nonagon
  - 10 sides - decagon

- Sum of exterior angles is always  $360^\circ$



- interior & exterior angle add up to  $180^\circ$

- the interior angles add up to:

Triangle =  $1 \times 180^\circ = 180^\circ$

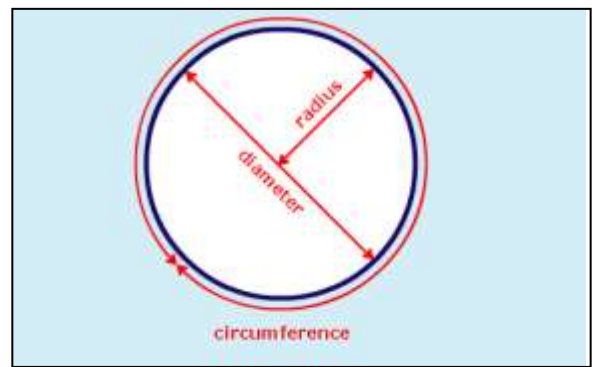
Quadrilateral =  $2 \times 180^\circ = 360^\circ$

Pentagon =  $3 \times 180^\circ = 540^\circ$

Hexagon =  $4 \times 180^\circ = 720^\circ$  etc

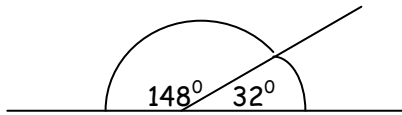
## 6/25 Parts of a circle

- The circumference is the distance all the way around a circle.
- The diameter is the distance right across the middle of the circle, passing through the centre.
- The radius is the distance halfway across the circle.
- The radius is always half the length of the diameter. ( $d = 2 \times r$ ) or ( $r = \frac{1}{2} \times d$ )



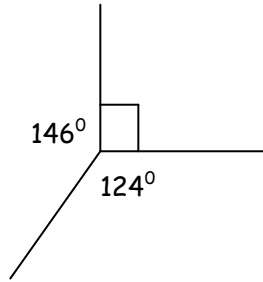
## 6/26 Angles and straight lines

- Angles on a straight line add up to  $180^\circ$



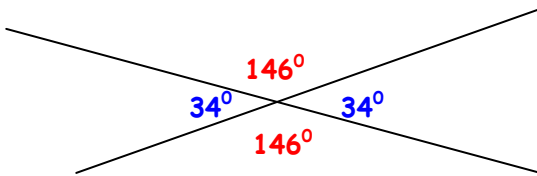
$$148^\circ + 32^\circ = 180^\circ$$

- Angles about a point add up to  $360^\circ$

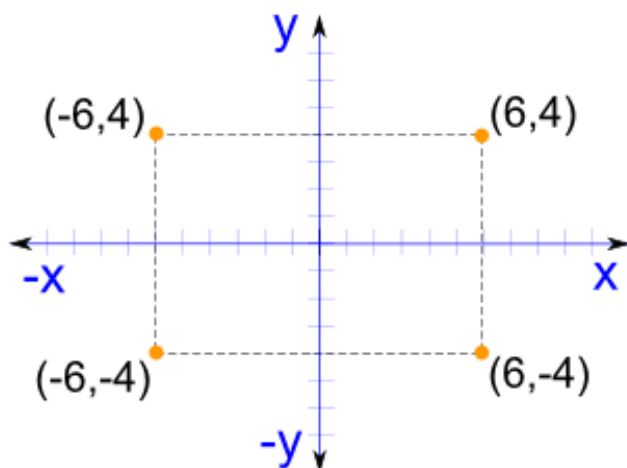


$$146^\circ + 90^\circ + 124^\circ = 360^\circ$$

- Vertically opposite angles are equal

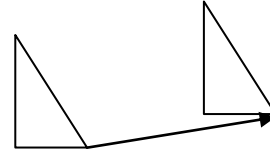


## 6/27 Position on a co-ordinate grid



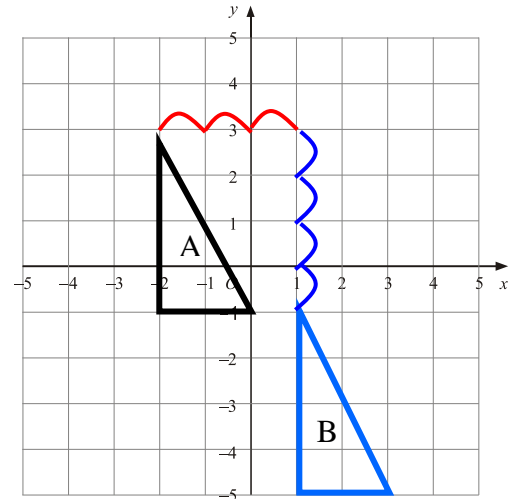
## 6/28 Transformations

- Translation** - A shape moved along a line



Example - Move shape A 3 right & 4 down

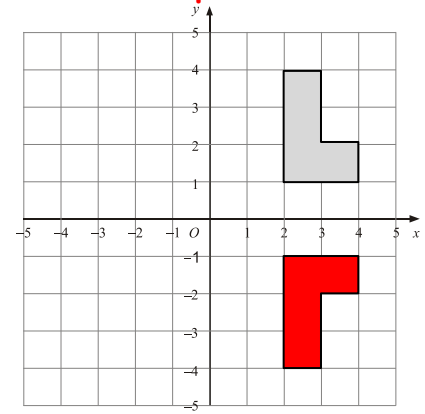
Can also be written as a vector  $\begin{pmatrix} 3 \\ -4 \end{pmatrix}$  Right Down



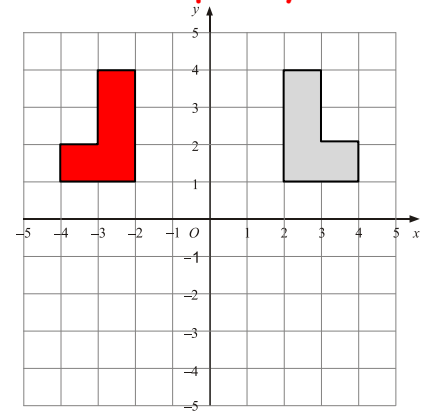
Notice:

- The new shape stays the same way up
- The new shape is the same size

- Reflect a shape in x-axis**



- Reflect a shape in y-axis**



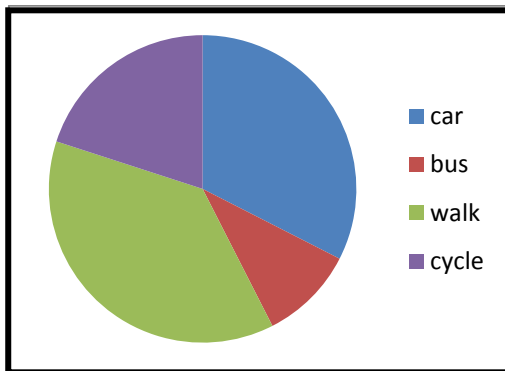


## 6/29 Graphs

### ○ Pie chart

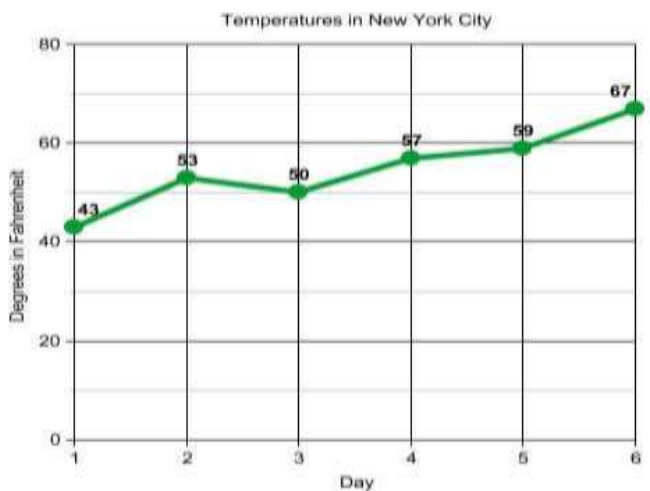
Transport	Frequency	Angle
Car	13	$13 \times 9 = 117^\circ$
Bus	4	$4 \times 9 = 36^\circ$
Walk	15	$15 \times 9 = 135$
Cycle	8	$8 \times 9 = 72$

↑  
Total frequency = 40  
 $360^\circ \div 40 = 9^\circ$  per person



### ○ Line graph

Line graphs show changes in a single variable - in this graph changes in temperature can be observed.



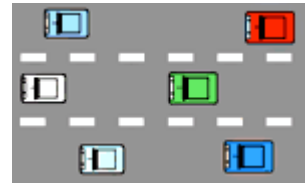
## 6/30 The mean

The mean is usually known as the average.  
The mean is not a value from the original list.  
It is a typical value of a set of data

Mean = total of measures  $\div$  no. of measures

e.g.- Find mean speed of 6 cars travelling on a road

Car 1 - 66mph  
Car 2 - 57mph  
Car 3 - 71mph  
Car 4 - 54mph  
Car 5 - 69mph  
Car 6 - 58mph



$$\begin{aligned} \text{Mean} &= \frac{66+57+71+54+69+58}{6} \\ &= \frac{375}{6} \\ &= 62.5\text{mph} \end{aligned}$$

Mean average speed was 62.5mph